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Quantum fluctuation effects on nuclear fragment formation[★]

Akira Ohnishi^{a,b}, Jørgen Randrup^b^a *Department of Physics, Faculty of Science, Hokkaido University, Sapporo 060, Japan*^b *Nuclear Science Division, Lawrence Berkeley National Laboratory, University of California, Berkeley, CA 94720, USA*

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Abstract

Multifragmentation in Au+Au collisions is investigated at incident energies in the range 100–400 MeV per nucleon by means of a recently developed quantal Langevin model. The inclusion of quantum fluctuations enhances the average multiplicity of intermediate mass fragments, especially in central collisions. This is mainly because the excitation energies of fragments are reduced due to the quantal behavior of intrinsic specific heat.

1. Introduction

One of the main goals of heavy-ion physics is to explore the various phases of nuclear matter and achieve an understanding of the associated phase transitions. At intermediate energies, the nuclear liquid-gas phase transition is of primary interest, and the efforts to understand this phenomenon have intensified following the recent extraction of a caloric curve of hot nuclear matter [1] suggesting that the phase transition is of first-order and occurs at a temperature of 4–5 MeV. The first-order nature of the phase transition may lead to an enhancement of fragment formation [2–4], since the rapid expansion following an energetic nucleus-nucleus collision causes a transformation from a hot to a supercooled gas phase. The resulting dilute system is mechanically unstable and fragments are there-

fore likely to be formed, in a manner similar to the formation of water drops.

The experimental exploration of nuclear phase transitions must rely on nuclear collisions, and it is therefore necessary to invoke dynamical models in the interpretation of the data. In addition to the complications arising from the non-equilibrium character of the collision dynamics, it is also important to ensure that the models employed take due account of the quantal nature of the nuclear system.

In order to illustrate this important point, we note that the nuclear liquid-gas phase transition differs significantly from the usual liquid-gas phase transition in macroscopic matter. The largest difference lies in the role played by quantal statistics. In the case of usual macroscopic matter, the total energies are to a good approximation linear functions of the temperature in both the liquid and gas phases. Thus the effective number of degrees of freedom is essentially constant in each phase. In contrast to this familiar situation, the liquid phase of a nucleus exhibits an increase in the number of activated degrees of freedom as the temperature is raised. For example, the excitation energy of a nucleus

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at low temperature increases like $E^* = aT^2$ (where the level density parameter is $a \approx A/(8 \text{ MeV})$), which is a typical quantal behavior, while the gas phase is characterized by the usual classical relation $E^*/A = 3T/2$. The two curves intersect at $T \approx 12 \text{ MeV}$, which is much higher than the suggested transition temperature. This indicates that the quantal statistical nature of the nuclear system plays an important role for the phase transition and, presumably, for the associated nuclear multifragmentation processes.

To take approximate account of the quantal features of the evolving nuclear system, we augment the so-called Quantum Molecular Dynamics (QMD) model [5–7] by a stochastic term given by the recently developed quantal Langevin model [8,9]. The QMD model describes the nuclear many-body system in terms of a product wave-function of gaussian wavepackets for the individual nucleons and has been successful in accounting for a variety of collision observables, such as collective flow and particle production [5]. The QMD model and its antisymmetrized versions, Antisymmetrized Molecular Dynamics (AMD) [10] and Fermionic Molecular Dynamics (FMD) [11], have also met with some success in describing fragment production [5,7,10,12–14]. The fragments formed in these molecular dynamics calculations are generally far too excited to remain intact, so the subsequent decay must be accounted for in order to extract the yield of bound fragments that are measured experimentally. This combination of molecular dynamics and subsequent (usually statistical) decay calculation may give us a correct picture of fragment formation when the source of fragments is limited to one compound nucleus or excited projectile-like and target-like fragments. However, when the copious intermediate-mass fragments (IMF) appear simultaneously, the above fragment formation mechanism becomes dubious. For example, although the calculated IMF multiplicity without the subsequent decay seems to reproduce the data reasonably [13,14], the decay processes largely eliminates the IMF yield [14].

We suggest that part of the reason for this consistent shortcoming of the entire class of QMD-like models may be found in the fact that the model is effectively classical, since the equations of motion for the wavepacket parameters have been derived by a standard variational principle. The resulting description is then the dynamics of the wavepacket centroids and the

inherent quantum fluctuations are neglected. The presence of quantum fluctuations is signaled by the fact that the wavepackets are not energy eigenstates. This basic feature generally causes the expectation value of the Hamiltonian to fluctuate in the course of time.

In order to remedy the situation, a quantal Langevin model was recently developed [8,9]. The Langevin force enables the wavepacket system to explore its entire energy spectral distribution, rather than being restricted to its average value, and it leads to a much improved description of the quantum statistical features. In particular, the resulting specific heat now exhibits the characteristic evolution from a quantum fluid towards a classical gas as a function of temperature [8,9], in contrast to the behavior emerging with the usual treatment. Since a change of a fragment's specific heat is associated with a change in its statistical weight, the effect is clearly relevant for the fragment production problem.

The key features of the results obtained with the quantal Langevin model are the occurrence of larger fluctuations and an enhancement of stable configurations, such as bound fragments, as a result of the need to take account of the spectral distortion of the wavepackets. The former feature arises from the fact that the wave packets are populated according to the strength of the eigenvector for the given energy, and therefore the wavepacket parameters can have larger fluctuations than when the expectation value of the energy is conserved. On the other hand, in order to project out the appropriate energy component from the wavepacket, it is necessary to take account of its internal distortion. The combination of these two basic features is then expected to enhance the IMF yield at the final stage: while the larger fluctuations allow the system to explore more configurations and thus enhances the yield of primary fragments, the latter stabilizes the fragments, since the compensation for the quantum distortion effectively acts as a cooling mechanism.

In our previous work [9], we have applied the quantal Langevin model to a simple soluble example and have shown that it leads to the correct quantal microcanonical equilibrium. However, in order to apply this model to actual nuclear collisions, the treatment of the center-of-mass cluster motion must be suitably modified. In the QMD and AMD treatments, the single-particle wave function is represented by a gaussian

wave packet with a fixed width. Then the center-of-mass wave function of each cluster is also a gaussian wave packet and, accordingly, it has zero-point kinetic energy as well as an energy fluctuation dependent on the velocity. Within the framework of the quantal Langevin model, this energy fluctuation causes a quantal fluctuation of the CM motion of the cluster even if it is well separated from other clusters and nucleons. This phenomenon reflects the expansion of a localized free wave packet and should be eliminated, as is usually done in Hartree-Fock and AMD calculations, for example, before the binding energy is calculated. In order not to modify the Q -values in the fragmentation process, the cluster CM motion must also be removed in the dynamical evolution, as was already discussed in Refs. [10,15]. Therefore, we have removed the energy fluctuation of the cluster center-of-mass motions as well. This can be accomplished by considering the motion of the individual nucleon constituents relative to the local collective velocity.

In this letter, we have included the quantal Langevin force into the framework of QMD. Although we have formulated the quantal Langevin model within the AMD framework, the appearance of the quantal fluctuation originates in the wave-packet nature of the many-body state and is therefore a general phenomenon. Thus the basic features of the model also apply to QMD which is easier to apply to heavier systems and we focus our attention on the fragmentation process in $^{197}\text{Au}+^{197}\text{Au}$ collisions. In this system, the total number of nucleons is so large that the statistical properties are expected to play a major role. In addition, the multiplicities of intermediate mass fragments are measured at incident energies of 100, 250, and 400 MeV per nucleon and their impact parameter dependence is also deduced [4]. The IMF multiplicities reach up to around ten, which is the largest number observed so far.

2. Quantal Langevin model at fixed temperature

We first give a condensed description of the recently introduced quantal Langevin model for the situation when the system can be regarded as being in thermal equilibrium at a given temperature.

The treatment seeks to take account of the energy fluctuations present in a system being described in

terms of many-body wave packets. As we have already discussed in detail in Ref. [9], this inherent energy dispersion modifies the statistical weight relative to the naive classical form,

$$\mathcal{W}_\beta(\mathbf{Z}) \equiv \langle \mathbf{Z} | \exp(-\beta \hat{H}) | \mathbf{Z} \rangle \neq \exp(-\beta \mathcal{H}) . \quad (1)$$

Here $\mathcal{H} = \langle \mathbf{Z} | \hat{H} | \mathbf{Z} \rangle$ is the expectation value of the Hamiltonian in the given wave-packet state $|\mathbf{Z}\rangle$ and thus the last quantity represent the usual classical statistical weight. The complex parameter set $\mathbf{Z} = \{z_1, z_2, \dots, z_A\}$ is related to the phase space coordinates in QMD, $z_n = \mathbf{r}_n/2\Delta r + i\mathbf{p}_n/2\Delta p$, where Δr and Δp are widths of wave packet. By invoking the harmonic approximation, it is possible to obtain a good description of the statistical weight by means of a simple “free energy”,

$$\mathcal{F}_\beta(\mathbf{Z}) \equiv -\log \mathcal{W}_\beta(\mathbf{Z}) = \frac{\mathcal{H}}{D} (1 - \exp(-\beta D)) , \quad (2)$$

where $D = \sigma_\pi^2/E^*$ is the effective level spacing. (The energy of the wave packet relative to its ground state is denoted by E^* and σ_π^2 is the associated variance.)

The relaxation towards this approximate quantal equilibrium can be described by the following Fokker-Planck equation for the distribution $\phi(\mathbf{Z})$ of wave-packet parameters,

$$\frac{D\phi}{Dt} = \left[-\sum_i \frac{\partial}{\partial q_i} V_i + \sum_{ij} \frac{\partial}{\partial q_i} M_{ij} \frac{\partial}{\partial q_j} \right] \phi , \quad (3)$$

$$V_i = -\sum_j M_{ij} \frac{\partial \mathcal{F}_\beta}{\partial q_j} , \quad (4)$$

where q_i represents either \mathbf{r}_n or \mathbf{p}_n . It is easy to check that the statistical equilibrium distribution, $\phi_{\text{eq}} = \exp(-\mathcal{F}_\beta)$, is a stationary solution to the above Fokker-Planck equation. Moreover, when the classical statistical weight is employed (*i.e.* when $\mathcal{F}_\beta^C = \beta \mathcal{H}$), the drift and the diffusion coefficients of the Fokker-Planck equation satisfy the usual Einstein relation, corresponding to $\alpha = 1$ in (5). On the other hand, when the quantal statistical weight obtained with the harmonic approximation is used, Eq. (2), the relation is modified. For example, if the effective level spacing

D does not depend strongly on the wave-packet parameters, the drift coefficient reduced by the factor α ,

$$V_i = -\alpha\beta \sum_j M_{ij} \frac{\partial \mathcal{H}}{\partial q_j},$$

$$\alpha = \frac{1 - \exp(-\beta D)}{\beta D}. \quad (5)$$

Since α is smaller than unity, the resulting Fokker-Planck equation gives smaller friction, thus in effect relatively larger fluctuations will arise.

It is convenient to solve the Fokker-Planck transport equation by means of a Langevin method. Within the framework of QMD the Langevin equation becomes

$$\dot{\mathbf{p}} = \mathbf{f} - \alpha\beta \mathbf{M}^p \cdot \mathbf{v} + \mathbf{g}^p \cdot \boldsymbol{\xi}^p, \quad (6)$$

$$\dot{\mathbf{r}} = \mathbf{v} + \alpha\beta \mathbf{M}^r \cdot \mathbf{f} + \mathbf{g}^r \cdot \boldsymbol{\xi}^r, \quad (7)$$

$$\mathbf{v} = \frac{\partial \mathcal{H}}{\partial \mathbf{p}}, \quad \mathbf{f} = -\frac{\partial \mathcal{H}}{\partial \mathbf{r}}, \quad (8)$$

$$\mathbf{M}^p = \mathbf{g}^p \cdot \mathbf{g}^p, \quad \mathbf{M}^r = \mathbf{g}^r \cdot \mathbf{g}^r. \quad (9)$$

Here \mathbf{r} and \mathbf{p} are the phase-space centroid parameters for the wave packet and $\boldsymbol{\xi}$ is used to denote random numbers drawn from a normal distribution with two a variance equal to two. In these equations, we have omitted the diffusion-induced drift term and that part of the mobility tensor that connects \mathbf{r} and \mathbf{p} .

2.1. Energy fluctuation

The key quantity in the quantal Langevin treatment is the energy dispersion σ_E^2 within each wave packet. In Refs. [8,9], the following approximate form was derived, σ_E^2 .

$$\sigma_E^2 = \frac{\partial \mathcal{H}}{\partial \mathbf{Z}} \cdot \mathbf{C}^{-1} \cdot \frac{\partial \mathcal{H}}{\partial \mathbf{Z}}$$

$$= \sum_n [\Delta r^2 \mathbf{f}_n \cdot \mathbf{f}_n + \Delta p^2 \mathbf{v}_n \cdot \mathbf{v}_n]. \quad (10)$$

Here the matrix \mathbf{C} arises from the antisymmetrization and, accordingly, it is the unit matrix in QMD. There are two problems in the application of the above expression to dynamical processes within the framework of QMD, such as nucleus-nucleus collisions. The first concerns the spurious zero-point center-of-mass motion of clusters and the second arises from the Pauli blocking, as we shall now discuss.

The energy fluctuation becomes larger when the wave packet moves faster, as should be the case, and it results from the zero-point kinetic energy of the fragment center of mass. The expression is adequate when the configuration volume is compact and all the degrees of freedom can be treated as wave packets. However, as is already discussed in Refs. [10,15], this zero-point CM kinetic energy is spurious and should be removed from the Hamiltonian. It must then also be removed from the energy fluctuation. In addition, it may be unreasonable to carry out the integral over all the parameter space near the given value, since no Pauli blocking effect is taken account of in the phase space parameters themselves in QMD. Then, it appears more physical to reduce the energy fluctuation according to the appropriate Pauli blocking factor. In order to satisfy these two requirements we have adopted the following form of the energy fluctuation,

$$\sigma_E^2 = \sum_n (1 - f_n)^2 [\Delta r^2 \mathbf{f}_n \cdot \mathbf{f}_n + \Delta p^2 (\mathbf{v}_n - \mathbf{u}_n) \cdot (\mathbf{v}_n - \mathbf{u}_n)]. \quad (11)$$

$$\mathbf{u}_i = \frac{1}{N_i} \sum_j c_{ij} \mathbf{v}_j. \quad (12)$$

The additional factor $(1 - f_n)^2$ represents the Pauli blocking for small changes, where f_n is the Wigner function. Here \mathbf{v}_j denotes the velocity of the nucleon j and the local flow velocity \mathbf{u}_i is obtained by performing a suitable smoothing, using $c_{ij} = \exp(-r_{ij}^2/4\Delta r^2)$ with $N_i = \sum_j c_{ij}$. The quantity entering in the energy fluctuation is then $\mathbf{v} - \mathbf{u}$, the velocity of a wave packet relative to the local collective flow, which represents those degrees of freedom having a wave packet nature.

On the other hand, the collective velocity \mathbf{u} , which is thought of as the cluster velocity, represents the degrees of freedom having a classical nature. The drift term of Eq. (6) is therefore modified accordingly,

$$\dot{\mathbf{p}} = \mathbf{f} - \alpha\beta \mathbf{M}^p \cdot (\mathbf{v} - \mathbf{u}) - \beta \mathbf{M}^p \cdot \mathbf{u} + \mathbf{g}^p \cdot \boldsymbol{\xi}^p. \quad (13)$$

It should be noted that when the energy fluctuation σ_E^2 is small, the above Langevin equation leads to the normal (classical) Langevin equation, $\dot{\mathbf{p}} = \mathbf{f} - \beta \mathbf{M}^p \cdot \mathbf{v} + \mathbf{g}^p \cdot \boldsymbol{\xi}^p$. This situation is realized when all the fragments are well separated and the intrinsic energy fluctuation is very small (*i.e.* all the fragments are close to their ground state).

In addition to modifying the statistical weight, the energy fluctuation also modifies the meaning of wave packet ensemble, since it causes a thermal distortion of the spectral strength distribution of the energy eigen-components within each wave packet. The distortion operator $\exp(-\beta\hat{H}/2)$ reduces the expectation value of the Hamiltonian in the particular state $|\mathbf{Z}\rangle$. The thermal distortion is calculated by replacing the time t by the imaginary time $i\tau$ in the equation of motion. The resulting “evolution” is then described by a cooling equation,

$$\frac{dp_n}{d\tau} = -\frac{2\Delta p^2}{\hbar} (v_n - u_n), \quad \frac{dr_n}{d\tau} = \frac{2\Delta r^2}{\hbar} f_n, \quad (14)$$

with which the state should be propagated until $\tau = \hbar\beta/2$. Here, v is again replaced by $v - u$ in order to leave the collective (or cluster) motion unaffected.

2.2. Fragmentation at fixed temperature

We have incorporated the above described quantal Langevin force into the QMD model. In the present implementation, the Gogny interaction [16] is used as the effective interaction. In addition, a correction for the fragment zero-point kinetic energy is included as described in Refs. [10,15]. Moreover, since the quantal Langevin force is sensitive to the minimum state of the given Hamiltonian, a Pauli potential [15,17] to guarantee that the nuclear sizes and bindings are reasonably reproduced by the model.

Fig. 1 shows the resulting mass distribution of fragments as obtained at various temperatures having a low average density (to ensure that the fragments are well separated). The results of the quantal Langevin model agree well with the grandcanonical calculation when $T \geq 4$ MeV. At lower temperatures, probably because of the limited functional space of QMD, both the quantal Langevin model and the classical Langevin model fail to describe the population of the heaviest fragments which in turn may lead to the overestimation of the proton multiplicity.

It is interesting to note that the mass distribution changes its appearance in the temperature region $T = 4 \sim 6$ MeV. At lower temperatures, a large part of the nucleons are bound in large fragments, while at higher temperatures, the lighter fragments grow abundant. This behavior reflects the transition from the excitation of various collective modes of heavy nuclei to

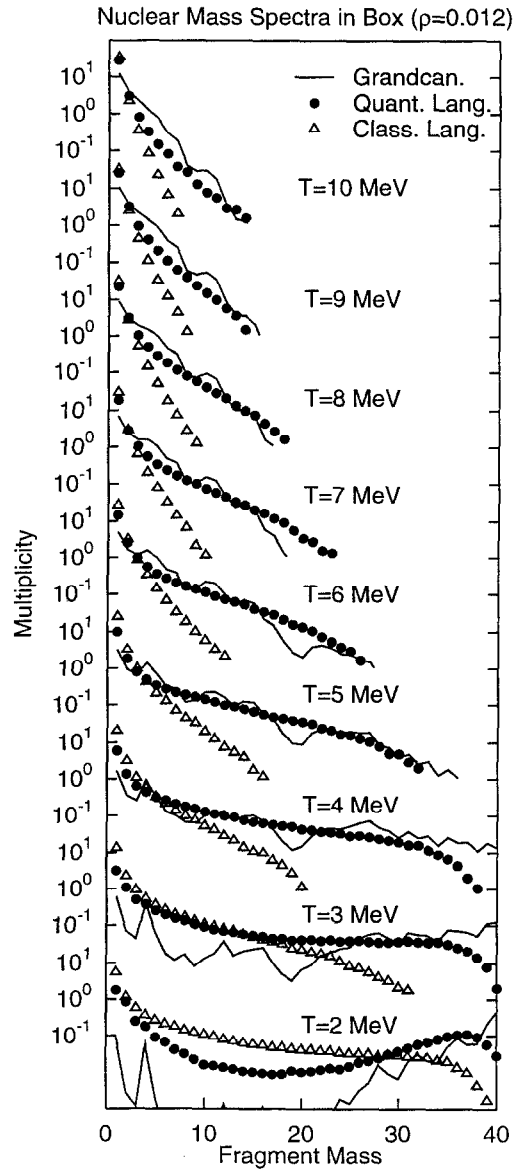


Fig. 1. Mass distribution in a canonical ensemble of 40 nucleons. Circles and triangles show the calculated results of QMD at the indicated temperatures T with ($\alpha < 1$) and without ($\alpha = 1$) the quantal modification. As an instructive reference for the quantal calculation, we also show the grand canonical results (solid lines) based on a simple statistical treatment [18].

the realization of fragmentation degrees of freedom. In our previous work [8,9], we have shown that this feature can be also seen from the relationship between temperature and excitation energy. The maximum specific heat is obtained for the temperature $T \sim 4$ MeV,

primarily because the fragment degrees of freedom are activated rapidly as T is increased above this value.

3. Application to nuclear collisions

In order to apply the treatment described above to actual nucleus-nucleus collision processes, some important modifications of the QMD model are required. In the usual QMD treatment, the expectation value of the Hamiltonian is a constant of motion (since the equations of motion for the wavepacket parameters have been derived from a standard variational principle). When the quantum fluctuations are taken into account, the inherent energy fluctuation within each many-body wavepacket makes it necessary to include wavepackets having different energy expectation values. At first, this feature might seem unreasonable as it appears to violate energy conservation. However, an energy eigenstate can be constructed as a superposition of wavepackets whose energy expectation values (the diagonal matrix elements of the Hamiltonian operator) are not necessarily the same as the energy eigenvalues. This feature grows more prominent in the reaction region and there is therefore no reason to exclude wavepackets with different energy expectation values in the dynamics, especially during the strongly interacting stage.

3.1. Quantal Fokker-Planck equation at a fixed energy

By proceeding as in the case considered above where the temperature is given, it is possible to derive a quantal Fokker-Planck equation for situations in which the energy is specified, such as the evolution of an isolated system. The equilibrium distribution is now a microcanonical ensemble, with a corresponding statistical weight for each wave packet,

$$\rho_E(\mathbf{Z}) \equiv \langle \mathbf{Z} | \delta(E - \hat{H}) | \mathbf{Z} \rangle \propto \frac{(\mathcal{H}/D)^{E/D}}{\Gamma(E/D + 1)} \exp(-\mathcal{H}/D). \quad (15)$$

The last relation assumes that the spectral function is given by a continuous Poisson distribution. The drift coefficient can then be readily calculated,

$$V_i = - \sum_j M_{ij} \frac{\partial \mathcal{F}_E}{\partial q_j} \simeq -\beta_{\mathcal{H}} \sum_j M_{ij} \frac{\partial \mathcal{H}}{\partial q_j}, \quad (16)$$

$$\mathcal{F}_E(\mathbf{Z}) \equiv -\log \rho_E(\mathbf{Z}), \quad (17)$$

$$\beta_{\mathcal{H}} \equiv \frac{\partial \mathcal{F}_E}{\partial \mathcal{H}} = \frac{\mathcal{H} - E}{\sigma_E^2}. \quad (18)$$

It is interesting to note that the drift term acts to restore the energy: when the Hamiltonian \mathcal{H} is greater than the given energy E , the drift term reduces the Hamiltonian (since $\beta_{\mathcal{H}}$ is positive in this case and the mobility tensor is always positive definite. Furthermore, since the phase volume with larger \mathcal{H} is larger, the dynamical trajectory usually goes through the region with $\mathcal{H} > E$. Therefore, the drift term generally reduces the excitation energy of fragments in the final stage of collision. In the asymptotic region where all the fragments are well separated and all of them are sufficiently cold, the energy fluctuation becomes small and the energy expectation value converges to the given value.

Thus, the basic features of the quantal Langevin model remain the same also in the case of a fixed energy, namely larger fluctuations and intrinsic distortion. To show this important point, we introduce the state-dependent microcanonical inverse temperature β_E , whose average over the entire phase space with the weight $\rho_E(\mathbf{Z})$ gives the global microcanonical temperature,

$$\beta_E(\mathbf{Z}) \equiv \frac{\partial}{\partial E} \log \rho_E(\mathbf{Z}) = -\frac{\partial}{\partial E} \mathcal{F}_E(\mathbf{Z}) \simeq \frac{1}{D} \log(\mathcal{H}/E). \quad (19)$$

The last relation holds when we employ the continuous Poisson distribution and the effective level spacing D is small compared to \mathcal{H} and E . In terms of this β_E , we have $\beta_{\mathcal{H}} = \alpha_E \beta_E$, with $\alpha_E = (1 - \exp(-\beta_E D)) / \beta_E D$. Thus the drift term is reduced by the factor α_E compared to the normal Einstein relation, in analogy with the canonical case of a fixed temperature.

3.2. Mobility tensor

Although the preceding statistical discussion gives the form of Fokker-Planck equation, including the modified fluctuation-dissipation relation, the mobility tensor must be determined separately. Although

the mobility tensor does not affect the equilibrium properties, it is important in a dynamical scenario since it determines the time scale. As we discussed in Refs. [8,9], this mobility tensor essentially represents the transition rate from the current dynamical state. This transition rate should be described by the residual interaction between nucleons, *i.e.* the off-diagonal part of the original Hamiltonian operator. In the present study, we have used the following relatively simple mobility tensor,

$$M_{ni,mj}^r = g \delta_{nm} \delta_{ij} \Delta r^2 \frac{\sigma_n^r}{\hbar} (1 - f_n), \quad (20)$$

$$M_{ni,mj}^p = g \delta_{nm} \delta_{ij} \Delta p^2 \frac{\sigma_n^p}{\hbar} (1 - f_n), \quad (21)$$

$$(\sigma_n^r)^2 = \Delta r^2 f_n \cdot f_n, \quad (22)$$

$$(\sigma_n^p)^2 = \Delta p^2 (v_n - u_n) \cdot (v_n - u_n). \quad (23)$$

Since the transition induced by the quantal Langevin force is of one-body nature, we have incorporated the blocking factor $1 - f_n$.

3.3. Results for Au+Au collisions

We have applied the quantal Langevin model to collisions of two gold nuclei at incident energies of 100, 250, and 400 MeV per nucleon. In addition to the Hamiltonian discussed above, an energy-conserving two-body collision term is also included. The average multiplicity of intermediate-mass fragments calculated for $^{197}\text{Au} + ^{197}\text{Au}$ is shown in the upper part of Fig. 2. The treatments with and without the quantal Langevin force agree with each other qualitatively. For example, the IMF multiplicity has the peak at central collisions at $E/A = 100$ MeV, while the peak moves to finite impact parameter at higher incident energies.

Since the fragments extracted from the dynamical calculations are still excited, it is necessary to include the subsequent statistical decay before contact with experiment can be made. The lower part of Fig. 2 shows the resulting average IMF multiplicity after the statistical decay chains have deexcited the fragments to below the light-fragment separation energy (we shall consider such relatively cold fragments as being in their ground states). As the statistical decay model (SDM), we have used the evaporation model of Pühlhofer [19]. In the case of QMD without quantal Langevin force, the excitation energies of the primary

fragments are large enough to largely eliminate the IMF component from the final mass distribution. This tendency is more clear for central collisions, where the fragments are likely to be highly excited. On the other hand, QMD with the quantal Langevin force reduces the excitation energies of the primary fragments because of the quantum-statistical nature of the intrinsic degrees of freedom. As a result, the difference between the average multiplicities before and after the statistical decay is less than one in the quantal Langevin model.

Although the difference between the two models seems small at $E/A = 100$ MeV, the IMF formation mechanisms are quite different. This feature becomes more clear when the ground state population is examined. With the quantal Langevin force, the primary fragments emerge relatively cold as a result of the drift term (the intrinsic distortion referred to above), while there is no other way than nucleon emission to cool fragments in the normal QMD model. Thus, the ground-state IMFs are more easily formed in the quantal Langevin model. A large part of the stable IMFs are created in the dynamical stage in the quantal Langevin model, whereas almost all the IMFs that appear with the usual QMD treatment owe their stability to the emission of particles during the statistical decay stage. Such a difference can, in principle, be subjected to measurement by exploiting the momentum correlation of the fragments.

4. Concluding remarks

In this paper, we have adapted the recently developed quantal Langevin model to simulations of nuclear collisions by embedding it into the widely used Quantum Molecular Dynamics model in which the individual nucleons are described by gaussian wave packets. The essential modification arises from the fact that the nuclear collision proceeds in isolation, so it is appropriate to consider the energy rather than the temperature to be fixed.

The essential effect of incorporating the quantal Langevin model is that the system exhibits larger fluctuations and the degree of excitation of the emerging fragments is smaller. These two features conspire to enhance the production of intermediate-mass fragments.

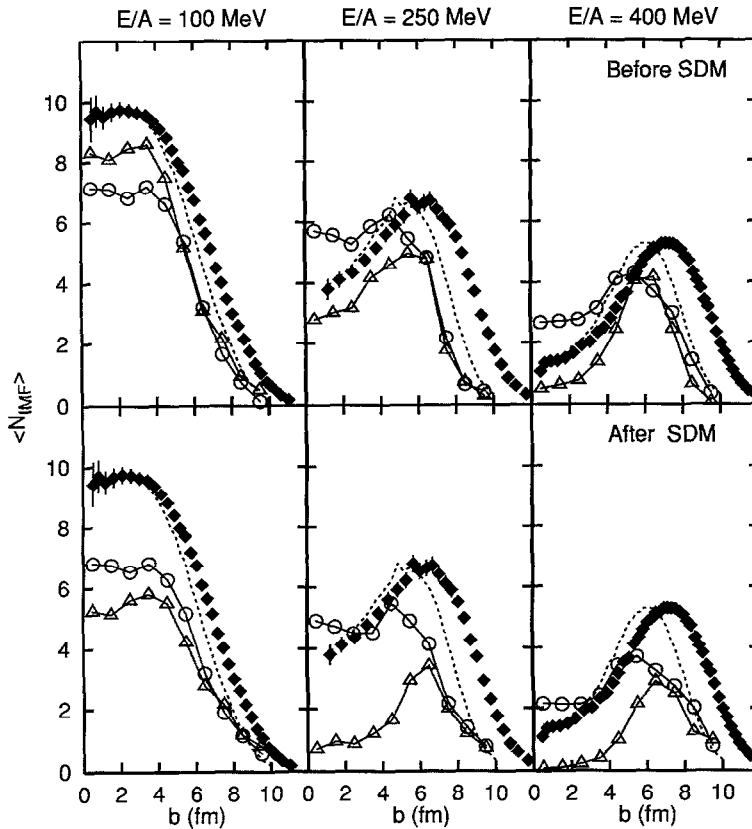


Fig. 2. IMF multiplicity before and after statistical decay. Circles and triangles indicate QMD results at given energies with and without the quantal Langevin force, respectively. The upper and lower parts show the distributions before and after the statistical decay (SDM) [19] calculation, respectively. The experimental data [4] are shown by solid diamonds. Dotted lines show the experimental data using a scaled impact parameter assuming a maximum impact parameter of 10 fm. The detector efficiency is not taken into account in the calculation.

The usual molecular-dynamics treatment leads to primary fragments that are typically sufficiently excited to emit nucleons. It is therefore essential to add an “afterburner” that subjects the unstable fragment to statistical decay. This process causes a strong suppression of the IMFs, and a corresponding enhancement of lighter fragments. Therefore, even though the usual dynamics leads to a large IMF multiplicity at the end of the dynamical stage [13,14], the final yields are not necessarily that large [14]. On the other hand, the quantum Langevin treatment leads to fragments having a relatively small degree of excitation and, consequently, a larger proportion of them survive the statistical decay.

The starting point for the present work was the fact that wave packet molecular dynamics displays classi-

cal statistical features, an observation that has stimulated lively discussion [8,9,15,20–23]. In our previous work [9], we demonstrated that when the mean energy is fixed molecular dynamics in a common harmonic oscillator potential may give the same observation with and without the quantal Langevin force. However, this coincidence depends strongly on the well-bound nature of the system and the calculated results in the present paper suggest that additional fluctuations are necessary to achieve a satisfactory molecular dynamics description of fragmentation processes. A similar conclusion has been reached by Ono and Horiuchi [24]. They included additional fluctuations to mimic the Vlasov dynamics in AMD, and also performed a constrained distortion of the wave function at each point in time. The combined effect of this ap-

proach seems to be rather similar to the two main features of the present quantal Langevin model.

Before it is possible to quantitatively assess the role played by the quantum nature of the system, it is necessary to resolve a number of important ambiguities in the quantal Langevin dynamics. For example, the mobility tensor adopted in this present work is based more on physical intuition than on first principles. Another ambiguity concerns the residual two-body collisions, since the quantal Langevin term causes the level density of the final state to differ from the classical one.

However, taken at face value, our results for Au+Au collisions indicate that the inclusion of the quantum fluctuations in the wavepacket dynamics leads to a significant increase in the production of massive fragments with low excitation. Although the experimental data are not yet reproduced quantitatively, the improvement is significant over the results obtained with the usual treatments in which the quantum fluctuations are ignored. This general qualitative result suggests that the underlying quantum nature of the nuclear many-body system may indeed play a significant role in fragmentation reactions.

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